

# Monad P3 : STRef Mutable Variable (3C)

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# Based on

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Haskell in 5 steps

[https://wiki.haskell.org/Haskell\\_in\\_5\\_steps](https://wiki.haskell.org/Haskell_in_5_steps)

# ST Monad

## Monad (**ST s**)

### Methods

**(>>=)** :: **ST s a** -> (**a** -> **ST s b**) -> **ST s b**

**(>>)** :: **ST s a** -> **ST s b** -> **ST s b**

**return** :: **a** -> **ST s a**

**fail** :: **String** -> **ST s a**

<https://hackage.haskell.org/package/base-4.9.0.0/docs/Data-STRef.html>

# STRef Mutable Variable

**Mutable references** in the (strict) **ST** monad.

**data STRef s a**

a **value** of type **STRef s a** is  
a **mutable variable** in **state thread s**,  
containing a **value** of type **a**

<https://hackage.haskell.org/package/base-4.9.0.0/docs/Data-STRef.html>

# IO, ST Monads and STRef Variable

```
newtype IO a = IO (State#(RealWorld) -> (# State#(RealWorld), a #))
```

```
newtype ST s a = ST (State#(s) -> (# State#(s), a #))
```

```
data STRef#(s, a) = STRef(MutVar#(s, a))
```

<https://haskell-lang.org/tutorial/primitive-haskell>

# **ST** Monad – no initial state parameter

there is no parameter for the **initial state** as in **State** monad

**ST** uses a different notion of state to **State**;

**State** allows you to **get** and **put** the current state,

**ST** provides an **interface** to references of the type **STRef**

**newSTRef** :: **a** -> **ST s (STRef s a)**

**readSTRef** :: **STRef s a** -> **ST s a**

**writeSTRef** :: **STRef s a** -> **a** -> **ST s ()**

[https://en.wikibooks.org/wiki/Haskell/Existentially\\_quantified\\_types](https://en.wikibooks.org/wiki/Haskell/Existentially_quantified_types)

# State Monad – providing the initial state

`get :: State s s`

`get = state $ \s -> (s, s)`

`runState (get) s0`

`runState (get) 1`

`(1,1)`

Initial state `s0` can be supplied either by `runState` or by the initial monadic value

`put :: s -> State s a`

`put s :: State s a`

`put newState = state $ \_ -> ((), newState)`

`runState (put ns) s0`

`runState (put 5) 1`

`(((),5)`

Initial state `s0` can be supplied either by `runState` or by the initial monadic value

[https://en.wikibooks.org/wiki/Haskell/Understanding\\_monads/State](https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State)

# Interface for a reference

- use the following **interfaces** (methods) to a **reference** (**STRef**)
- to create **references** of the type **STRef**,
- to provide an **initial value** and to **manipulate** them

`newSTRef :: a -> ST s (STRef s a)`

`readSTRef :: STRef s a -> ST s a`

`writeSTRef :: STRef s a -> a -> ST s ()`

[https://en.wikibooks.org/wiki/Haskell/Existentially\\_quantified\\_types](https://en.wikibooks.org/wiki/Haskell/Existentially_quantified_types)

# Mapping from references to values

`runST :: forall a. (forall s. ST s a) -> a`

`newSTRef :: a -> ST s (STRef s a)`

`readSTRef :: STRef s a -> ST s a`

`writeSTRef :: STRef s a -> a -> ST s ()`

the **internal environment** of a **ST computation**  
is not one **specific value**,  
but a **mapping from references to values**.

`runST`

`a ... STRef s a`



[https://en.wikibooks.org/wiki/Haskell/Existentially\\_quantified\\_types](https://en.wikibooks.org/wiki/Haskell/Existentially_quantified_types)

# Start with empty mapping

`runST :: forall a. (forall s. ST s a) -> a`

no need to provide an **initial state** to `runST`, ..... `s`

as the **initial state** is

just the **empty mapping** containing no references.

```
runST (do
    ref <- newSTRef "hello"
    x <- readSTRef ref
    writeSTRef ref (x ++ "world")
    readSTRef ref)
```

Start with an **empty mapping**  
– **no reference**

**no ST computation** should be allowed to assume that  
the **initial internal environment** contains **any specific references**.

[https://en.wikibooks.org/wiki/Haskell/Existentially\\_quantified\\_types](https://en.wikibooks.org/wiki/Haskell/Existentially_quantified_types)

# Reference in a ST computation

creating a **reference** in one ST computation,

It cannot be used in another ST computation

We don't want to allow this because of **thread-safety**

Example: Bad ST code

```
let v = runST (newSTRef True)  
in runST (readSTRef v)
```

*Two ST computations*

Valid ST code

```
runST (do  
    ref <- newSTRef "hello"  
    x <- readSTRef ref  
    writeSTRef ref (x ++ "world")  
    readSTRef ref )
```

*One ST computations*

[https://en.wikibooks.org/wiki/Haskell/Existentially\\_quantified\\_types](https://en.wikibooks.org/wiki/Haskell/Existentially_quantified_types)

# ST Monad Usage Example

```
import Data.STRef
import Control.Monad
import Data.Vector.Unboxed.Mutable as M
import Data.Vector.Unboxed as V

sumST :: Num a => [a] -> a
sumST xs = runST $ do
    n <- newSTRef 0
    Control.Monad.forM_ xs $ \x ->
        modifySTRef n (+x)
    readSTRef n
```

```
makeArray = runST $ do
    n <- newSTRef [1,2,3]
    readSTRef n

makeArray' = newSTRef 10 >>= readSTRef

makeArray'' = do
    a <- newSTRef 10
    b <- newSTRef 11
    return (a,b)

makeVec = runST $ do
    v <- M.replicate 3 (1.2::Double)
    write v 1 3.1
    V.freeze v
```

<http://www.philipzucker.com/simple-st-monad-examples/>

# Example sumST

```
import Control.Monad.ST
import Data.STRef
import Control.Monad

sumST :: Num a => [a] -> a
sumST xs = runST $ do
    summed <- newSTRef 0
    forM_ xs $ \x -> do
        modifySTRef summed (+x)
    readSTRef summed
-- runST takes stateful ST code and makes it pure.
-- Create an STRef (a mutable variable)
-- For each element of the argument list xs ..
-- add it to what we have in n.
-- read the value of n, which will be returned by the runST above.
```

[https://en.wikipedia.org/wiki/Haskell\\_features#ST\\_monad](https://en.wikipedia.org/wiki/Haskell_features#ST_monad)

# No leak information about **n** and **s**

**sumST** is no less **pure** than the familiar **sum**.

The fact that it destructively updates its accumulator **n** is a mere implementation detail,

there is no way information about **n** could leak except through the final result.

the **s** type variable in **ST s a** does not correspond to anything in particular within the computation – it is just an **artificial marker**.

```
sumST :: Num a => [a] -> a
sumST xs = runST $ do
    n <- newSTRef 0
    forM_ xs $ \x ->
        modifySTRef n (+x)
    readSTRef n
```

```
newSTRef :: a -> ST s (STRef s a)
readSTRef :: STRef s a -> ST s a
writeSTRef :: STRef s a -> a -> ST s ()
n :: STRef s a
```

[https://en.wikibooks.org/wiki/Haskell/Mutable\\_objects](https://en.wikibooks.org/wiki/Haskell/Mutable_objects)

# forM\_ from the left

even though **forM\_** folds the list from the right  
the **sums** are done from the left,

as the mutations are performed as **applicative** effects  
sequenced **from left to right**.

```
sumST :: Num a => [a] -> a
sumST xs = runST $ do
    n <- newSTRef 0
    forM_ xs $ \x ->
        modifySTRef n (+x)
    readSTRef n
```

```
modifySTRef :: STRef s a ->
    (a -> a) -> ST s ()
n :: STRef s a
(+x) :: a -> a
modifySTRef n (+x) :: ST s ()
```

[https://en.wikibooks.org/wiki/Haskell/Mutable\\_objects](https://en.wikibooks.org/wiki/Haskell/Mutable_objects)

# Return value

`runST :: (forall s. ST s a) -> a`

return the **value** computed  
by a **state transformer computation**.

The **forall** ensures that the **internal state**  
used by the **ST computation**  
is inaccessible to the rest of the program.

... **s**  
... `runST $ do ...`

`sumST :: Num a => [a] -> a`

`sumST xs = runST $ do`

`n <- newSTRef 0`

`forM_ xs $ \x ->`

`modifySTRef n (+x)`

`readSTRef n`

`n :: STRef s a`

`readSTRef :: STRef s a -> ST s a`

`readSTRef n :: ST s a`

`do ... readSTRef n :: ST s a`

`runST $ do ... readSTRef n :: a`

<https://wiki.haskell.org/Monad/ST>

# STRef – not strict modifying

Be warned that **modifySTRef** does not apply the function **strictly**.

if the program calls **modifySTRef** many times,  
but seldomly uses the **value**,  
**thunks** will pile up in memory resulting in a **space leak**.

do not use an **STRef** as a **counter**.

**Memory leak** example (likely produce a stack overflow)

```
print $ runST $ do
    ref <- newSTRef 0
    replicateM_ 1000000 $ modifySTRef ref (+1)
    readSTRef ref
```

<https://hackage.haskell.org/package/base-4.9.0.0/docs/Data-STRef.html>

# Operations on **MutVar#**'s

**data MutVar# s a**

A **MutVar#** behaves like a single-element mutable array.

**newMutVar# :: a -> State# s -> (#State# s, MutVar# s a#)**

Create **MutVar#** with specified **initial value** in specified **state thread**.

**readMutVar# :: MutVar# s a -> State# s -> (#State# s, a#)**

Read contents of **MutVar#**. Result is not yet evaluated.

**writeMutVar# :: MutVar# s a -> a -> State# s -> State# s**

Write contents of **MutVar#**.

**sameMutVar# :: MutVar# s a -> MutVar# s a -> Bool**

<https://downloads.haskell.org/~ghc/7.2.2/docs/html/libraries/ghc-prim-0.2.0.0/GHC-Prim.html#t:State-35>

# Operations on **MutVar#**'s – source

```
data MutVar#(s, a)

newMutVar#(a) :: a -> State#(s) -> (# State#(s), MutVar#(s, a) #)
newMutVar#(a) = let x = x in x

readMutVar#(a) :: MutVar#(s, a) -> State#(s) -> (# State#(s), a #)
readMutVar#(a) = let x = x in x

writeMutVar#(a) :: MutVar#(s, a) -> a -> State#(s) -> State#(s)
writeMutVar#(a) = let x = x in x

sameMutVar#(a) :: MutVar#(s, a) -> MutVar#(s, a) -> Bool
sameMutVar#(a) = let x = x in x
```

<https://downloads.haskell.org/~ghc/7.2.2/docs/html/libraries/ghc-prim-0.2.0.0/src/GHC-Prim.html#MutVar%23>

# STRef Definition (1)

```
data STRef#(s, a) = STRef(MutVar#(s, a))  
-- ^ a value of type @STRef#(s, a)@ is a mutable variable in state thread @s@,  
-- containing a value of type @a@  
--  
-- >>> :{  
-- runST (do  
--   ref <- newSTRef "hello"  
--   x <- readSTRef ref  
--   writeSTRef ref (x ++ "world")  
--   readSTRef ref )  
-- }  
-- "helloworld"
```

**newtype ST#(s, a) = ST(State#(s) -> (# State#(s), a #))**

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# STRef Definition (2)

```
- | A value of type `STRef s a` is a mutable variable in state thread `s`,  
-- containing a value of type `a`
```

```
data STRef#(s, a) = STRef#(MutVar#(s, a))
```

```
-- |Build a new 'STRef' in the current state thread
```

```
newSTRef :: a -> ST#(s, STRef#(s, a))
```

```
newSTRef#(init) = ST#(s, MutVar#(s, a))()
```

```
case newMutVar#(init) s1#(a) of
```

```
{(s2#, var#(a)) -> (s2#, STRef#(a))}
```

<https://osa1.net/posts/2016-07-25-IORef-STRef-exposed.html>

# STRef Definition (3)

```
-- | Read the value of an 'STRef'  
readSTRef :: STRef s a -> ST s a  
readSTRef (STRef var#) = ST $ \s1# -> readMutVar# var# s1#  
  
-- | Write a new value into an 'STRef'  
writeSTRef :: STRef s a -> a -> ST s ()  
writeSTRef (STRef var#) val = ST $ \s1# ->  
  case writeMutVar# var# val s1# of  
    { s2# -> (# s2#, () #) }
```

Note that there's no atomicModifySTRef, because that only makes sense in IO context. So atomicModifyIORef directly calls the primop.

<https://osa1.net/posts/2016-07-25-IORef-STRef-exposed.html>

# newSTRef method (1)

```
-- |Build a new 'STRef' in the current state thread
newSTRef :: a -> ST s (STRef s a)
newSTRef init = ST $ \s1# ->
  case newMutVar#(init s1#) of
    { (# s2#, var# #) -> (# s2#, STRef var# #) }
```

init :: a  
s1# :: State# s  
s2# :: State# s  
var# :: MutVar# s a

```
data STRef#(s, a) = STRef(MutVar#(s, a))
newtype ST#(s, a) = ST(State#(s) -> (# State#(s), a #))
newMutVar#::(a) -> State#(s) -> (# State#(s), MutVar#(s, a) #)
```

s1# is transformed into s2#  
which is embedded into var#

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# newSTRef method (2)

```
newSTRef :: a -> ST s (STRef s a)
```

```
newSTRef init = ST $ \s1# ->  
  case newMutVar# init s1# of  
    { (# s2#, var# #) -> (# s2#, STRef var# #) }
```

```
newMutVar# :: a -> State# s -> (# State# s, MutVar# s a #)
```

```
newMutVar# init s1# :: (# State# s, MutVar# s a #)
```

init :: a

s1# :: State# s

init :: a

s1# :: State# s

s2# :: State# s

var# :: MutVar# s a

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# newSTRef method (3)

```
newSTRef :: a -> ST s (STRef s a)
```

```
newSTRef init = ST $ \s1# ->  
  case newMutVar# init s1# of  
    { (# s2#, var# #) -> (# s2#, STRef var# #) }
```

(pattern matching)

```
newMutVar# :: a -> State# s -> (# State# s, MutVar# s a #)
```

```
newMutVar# init s1# :: (# State# s, MutVar# s a #)
```

```
(# s2#, var# #) :: (# State# s, MutVar# s a #)
```

```
  s2# :: State# s
```

```
  var# :: MutVar# s a
```

init :: a

s1# :: State# s

s2# :: State# s

var# :: MutVar# s a

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# newSTRef method (4)

```
newSTRef :: a -> ST s (STRef s a)
```

```
newSTRef init = ST $ \s1# ->  
  case newMutVar#(init) s1# of  
    { (# s2#, var# #) -> (# s2#, STRef var# #) }
```

```
newSTRef init = ST $ \s1# -> (# s2#, STRef var# #)
```

memorization purpose

```
data STRef#(s, a) = STRef#(MutVar#(s, a))
```

```
STRef#(var#) :: STRef#(s, a)
```

```
newtype ST#(s, a) = ST#(State#(s) -> (# State#(s), a #))
```

```
ST$ \s1# -> (# s2#, STRef var# #) :: ST#(s, a) (STRef#(s, a))
```

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# newSTRef method (5)

```
newSTRef :: a -> ST s (STRef s a)
```

```
newSTRef init = ST $ \s1# ->  
  case newMutVar# init s1# of  
    { (# s2#, var# #) -> (# s2#, STRef var# #) }
```

```
newSTRef init = ST $ \s1# -> (# s2#, STRef var# #)
```

```
newSTRef init :: ST s (STRef s a)
```

s1# is transformed into s2# which is embedded into var#

memorization purpose

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# readSTRef method (1)

```
-- | Read the value of an 'STRef'
```

```
readSTRef :: STRef#(s, a) -> ST#(s, a)
```

```
readSTRef(STRef var#) = ST\$!s1# -> readMutVar#(var#)(s1#)
```

s1# :: State#(s)

var# :: MutVar#(s, a)

(**STRef** var#)

(pattern matching)

```
data STRef#(s, a) = STRef(MutVar#(s, a))
```

```
newtype ST#(s, a) = ST(State#(s) -> (#State#(s), a#))
```

```
readMutVar#(:: MutVar#(s, a) -> State#(s) -> (#State#(s), a#))
```

  
s1# is transformed into s2#  
extract the embedded value in var#

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# readSTRef method (2)

```
readSTRef :: STRef s a -> ST s a  
readSTRef (STRef var#) = ST $ !s1# -> readMutVar# var# s1#
```

(pattern matching)

```
data STRef s a = STRef (MutVar# s a)  
STRef (MutVar# s a) :: STRef s a  
STRef var# :: STRef s a  
var# :: MutVar# s a
```

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# readSTRef method (3)

```
readSTRef :: STRef s a -> ST s a  
readSTRef (STRef var#) = ST $ \s1# -> readMutVar# var# s1#
```

```
newtype ST s a = ST (State# s -> (# State# s, a #))
```

```
ST (State# s -> (# State# s, a #)) :: ST s a
```

```
ST $ \s1# -> readMutVar# var# s1# :: ST s a
```

```
s1# :: State# s
```

```
readMutVar# var# s1# :: (# State# s, a #)
```

```
readMutVar# :: MutVar# s a -> State# s -> (# State# s, a #)
```

```
var# :: MutVar# s a
```

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# readSTRef method (4)

```
readSTRef :: STRef s a -> ST s a
```

```
readSTRef (STRef var#) = ST $ \s1# -> readMutVar# var# s1#
```

```
readMutVar# :: MutVar# s a -> State# s -> (# State# s, a #)
```

var# :: MutVar# s a

```
readMutVar# var# s1# = (# s2# val #)
```

val :: a

**memorization purpose**

val is the embedded value in var#

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# readSTRef method (5)

```
readSTRef :: STRef s a -> ST s a
```

```
readSTRef (STRef var#) = ST $ \s1# -> readMutVar# var# s1#
```

```
readSTRef (STRef var#) = ST $ \s1# -> (# s2# , val #)
```

```
readSTRef (STRef var#) :: ST s a
```

**memorization purpose**

s1# is transformed into s2#  
extract the embedded value in var#

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# writeSTRef method (1)

```
-- |Write a new value into an 'STRef'  
writeSTRef :: STRef s a -> a -> ST s ()  
writeSTRef (STRef var#) val = ST $ \s1# ->  
  case writeMutVar# var# val s1# of  
    { s2# -> (# s2#, () #) }
```

s1# :: State# s  
s2# :: State# s  
var# :: MutVar# s a  
val :: a

(STRef var#)  
(pattern matching)

```
data STRef s a = STRef (MutVar# s a)  
newtype ST s a = ST (State# s -> (# State# s, a #))  
writeMutVar# :: MutVar# s a -> a -> State# s -> State# s
```

s1# is transformed into s2#  
change the embedded value in var#

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# writeSTRef method (2)

```
writeSTRef :: STRef#(a, a) -> a
```

```
writeSTRef(STRef#(a, a) var#, a val) = ST$!(var#(a, a)) ->
    case writeMutVar#(a, a)(var#, a val) of
        { a s2#, Action action } => action
```

(pattern matching)

```
writeMutVar#(a, a) :: MutVar#(a, a) -> a
```

```
writeMutVar#(a, a) var#, a val
```

```
var# :: MutVar#(a, a)
```

```
a val
```

```
s1# :: State#(a)
```

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# writeSTRef method (3)

```
writeSTRef :: STRef#(a, a) -> a
writeSTRef(STRef#(a, a) var#, a val) = ST $ \s1# ->
    case writeMutVar#(a, a)(var#, val, s1#) of
        { a s2# -> (# s2#, 0 #) }
```

```
writeMutVar#(a, a) :: MutVar#(a, a) -> a
writeMutVar#(a, a) var#, a val, a s1#(a, a) -> a s2#(a, a)
```

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# writeSTRef method (4)

```
writeSTRef :: STRef#(a, a) write(a)
```

```
writeSTRef(STRef#(var)) val = ST $ \s1# ->  
  case writeMutVar#(var) val s1# of  
    { s2# -> (# s2#, () #) }
```

```
writeSTRef(STRef#(var)) val = ST $ \s1# -> (# s2#, () #)
```

memorization purpose

```
newtype ST#(a) = ST#(State#(a) state, a value)
```

```
ST $ \s1# -> (# s2#, () #) :: ST#(a)
```

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# writeSTRef method (5)

```
writeSTRef :: STRef s a -> a -> ST s ()
```

```
writeSTRef (STRef var#) val = ST $ \s1# ->  
  case writeMutVar# var# val s1# of  
    { s2# -> (# s2#, () #)}
```

```
writeSTRef (STRef var#) val = ST $ \s1# -> (# s2#, () #)
```

```
writeSTRef :: STRef s a -> a -> ST s ()
```

**memorization purpose**

s1# is transformed into s2#  
change the embedded value in var#

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# Summary (1)

```
newSTRef init = ST $ \s1# -> (# s2#, STRef var# #)
```

```
newSTRef init :: ST s (STRef s a)
```

```
readSTRef (STRef var#) = ST $ \s1# -> (# s2#, val #)
```

```
readSTRef (STRef var#) :: ST s a
```

```
writeSTRef (STRef var#) val = ST $ \s1# -> (# s2#, () #)
```

```
writeSTRef :: STRef s a -> a -> ST s ()
```

**STRef var# :: STRef s a**

**var# :: MutVar# s a**

**memorization purpose**

s1# is transformed into s2#  
which is embedded into var#

**memorization purpose**

s1# is transformed into s2#  
extract the embedded value in var#

**memorization purpose**

s1# is transformed into s2#  
change the embedded value in var#

```
data STRef s a = STRef (MutVar# s a)
```

```
newtype ST s a = ST (State# s -> (# State# s, a #))
```

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# Summary (2)

```
newSTRef init = ST $ \s1# -> (# s2#, STRef var# #)
```

```
newMutVar# :: a -> State# s -> (# State# s, MutVar# s a #)
```

```
readSTRef (STRef var#) = ST $ \s1# -> (# s2#, val #)
```

```
readMutVar# :: MutVar# s a -> State# s -> (# State# s, a #)
```

```
writeSTRef (STRef var#) val = ST $ \s1# -> (# s2#, () #)
```

```
writeMutVar# :: MutVar# s a -> a -> State# s -> State# s
```

STRef var# :: STRef s a

var# :: MutVar# s a

```
data STRef s a = STRef (MutVar# s a)
```

```
newtype ST s a = ST (State# s -> (# State# s, a #))
```

**memorization purpose**

s1# is transformed into s2# which is embedded into var#

**memorization purpose**

s1# is transformed into s2# extract the embedded value in var#

**memorization purpose**

s1# is transformed into s2# change the embedded value in var#

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# Mutable reference interface

```
newSTRef :: a -> ST s (STRef s a)
```

```
readSTRef :: STRef s a -> ST s a
```

```
writeSTRef :: STRef s a -> a -> ST s ()
```

```
newSTRef init = ST $ \s1# -> (# s2#, STRef var# #)
```

```
readSTRef (STRef var#) = ST $ \s2# -> (# State# s3#, val #)
```

```
writeSTRef (STRef var#) val = ST $ \s3# -> (# s4#, () #)
```

```
STRef var# :: STRef s a
```

```
var# :: MutVar# s a
```

```
data STRef s a = STRef (MutVar# s a)
```

```
newtype ST s a = ST (State# s -> (# State# s, a #))
```

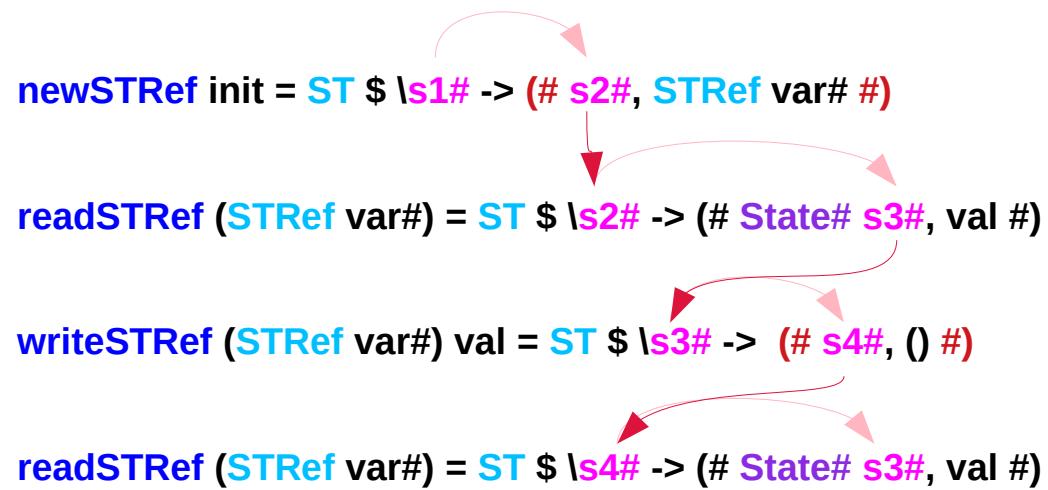
\* memorization purpose

mutable references in the ST monad  
are possible through threading state  
s1#, s2#, s3#, ...

[https://en.wikibooks.org/wiki/Haskell/Mutable\\_objects](https://en.wikibooks.org/wiki/Haskell/Mutable_objects)

# testST example – imperative style

```
runST (do  
    ref <- newSTRef 0  
  
    x <- readSTRef ref  
  
    writeSTRef ref (x + 3)  
  
    readSTRef ref )
```



[https://en.wikibooks.org/wiki/Haskell/Mutable\\_objects](https://en.wikibooks.org/wiki/Haskell/Mutable_objects)

# Instance Eq

```
-- | Pointer equality.  
--  
-- @since 2.01  
instance Eq (STRef s a) where  
    STRef v1# == STRef v2# = isTrue# (sameMutVar#(v1#, v2#))
```

<http://hackage.haskell.org/package/base-4.12.0.0/docs/src/GHC.STRef.html#STRef>

# MutVar

```
data MutVar s a
```

A MutVar behaves like a single-element mutable array associated with a primitive state token.

## Constructors

**MutVar** (**MutVar#** s a)

<http://hackage.haskell.org/package/primitive-0.7.0.0/docs/Data-Primitive-MutVar.html>

# MutVar Methods

**newMutVar :: PrimMonad m => a -> m (MutVar (PrimState m) a)**

Create a new MutVar with the specified initial value

**readMutVar :: PrimMonad m => MutVar (PrimState m) a -> m a**

Read the value of a MutVar

**writeMutVar :: PrimMonad m => MutVar (PrimState m) a -> a -> m ()**

Write a new value into a MutVar

<http://hackage.haskell.org/package/primitive-0.7.0.0/docs/Data-Primitive-MutVar.html>

# PrimState m

```
class Monad m => PrimMonad m where
```

Class of monads which can perform primitive state-transformer actions

Associated Types

```
type PrimState m
```

state token type

Methods

```
primitive :: (#State# (PrimState m) -> (#State# (PrimState m), a#)) -> m a
```

Execute a primitive operation

<http://hackage.haskell.org/package/primitive-0.7.0.0/docs/Control-Monad-Primitive.html#t:PrimMonad>

# STRef Definition

```
class Monad m => PrimMonad m where
```

Class of monads which can perform primitive state-transformer actions

Associated Types

```
type PrimState m
```

State token type

Methods

```
primitive :: (State#(PrimState m) -> (#State#(PrimState m), a#)) -> m a
```

Execute a primitive operation

<http://hackage.haskell.org/package/primitive-0.7.0.0/docs/Control-Monad-Primitive.html#t:PrimMonad>

## References

- [1] <ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf>
- [2] <https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf>