

x	y	z	Minterm		Maxterm	
			term		term	
0	0	0	$x'y'z'$	m0	$(x+y+z)$	M0
1	0	1	$x'y'z$	m1	$(x+y+z')$	M1
2	0	1	$x'yz'$	m2	$(x+y'+z)$	M2
3	0	1	$x'yz$	m3	$(x+y'+z')$	M3
4	1	0	$xy'z'$	m4	$(x'+y+z)$	M4
5	1	0	$xy'z$	m5	$(x'+y+z')$	M5
6	1	1	xyz'	m6	$(x'+y'+z)$	M6
7	1	1	xyz	m7	$(x'+y'+z')$	M7

$$\begin{array}{l|l} \text{x=0 and y=0 and z=0} & \longleftrightarrow x'y'z'=1 \\ \text{x=0 and y=0 and z=1} & \longleftrightarrow x'y'z=1 \end{array}$$

$$\begin{array}{l|l} \text{x=0 and y=0 and z=0} & \longleftrightarrow (x+y+z)=0 \\ \text{x=0 and y=0 and z=1} & \longleftrightarrow (x+y+z')=0 \end{array}$$

A	B	C	D	minterm	maxterm
0	1	1	0	$A'BCD'$	$A+B'+C'+D$
1	0	1	1	$AB'CD$	$A'+B+C'+D'$

$$f_1 = x'y'z + xy'z' + xyz = m1 + m4 + m7$$

In order f_1 has the value of 1,
the following minterms should be included
($m1=1$) or ($m4=1$) or ($m7=1$)

m0, m2, m3, m5, m6

$$m0 + m2 + m3 + m5 + m6 = x'y'z' + x'yz' + x'yz + xy'z + xyz' = f_1'$$

$$(m0 + m2 + m3 + m5 + m6)' = (x'y'z' + x'yz' + x'yz + xy'z + xyz')' = (f_1')'$$

De Morgan's law

$$f_1 = (m_0 + m_2 + m_3 + m_5 + m_6)' = (x'y'z' + x'yz' + x'yz + xy'z + xyz')'$$

$$f_1 = (m_0' m_2' m_3' m_5' m_6') = (x'y'z')' (x'yz')' (x'yz)' (xy'z)' (xyz')'$$

De Morgan's law

$$f_1 = (m_0' m_2' m_3' m_5' m_6') = (x+y+z) (x+y'+z) (x+y'+z') (x'+y+z) (x'+y'+z)$$

$$f_1 = (m_0' m_2' m_3' m_5' m_6') = (M_0) (M_2) (M_3) (M_5) (M_6)$$

$$f_1 = (m_0' m_2' m_3' m_5' m_6') = (m_0=0) \wedge (m_2=0) \wedge (m_3=0) \wedge (m_5=0) \wedge (m_6=0)$$

in order to f_1 has the value of 1,

the following **minterms** should not be included

m_0, m_2, m_3, m_5, m_6

$$f_1 = (M_0) (M_2) (M_3) (M_5) (M_6) = (M_0=1) \wedge (M_2=1) \wedge (M_3=1) \wedge (M_5=1) \wedge (M_6=1)$$

in order to f_1 has the value of 1,

the following **maxterms** should not be included

M_0, M_2, M_3, M_5, M_6

Sum of Product Sum of Minterms

$$f_1 = x'y'z + xy'z' + xyz = m_1 + m_4 + m_7 \quad \text{SoP}$$

$$\begin{aligned} f_1 &= (m_0' m_2' m_3' m_5' m_6') = M_0 M_2 M_3 M_5 M_6 \\ &= (x+y+z) (x+y'+z) (x+y'+z') (x'+y+z) (x'+y'+z) \end{aligned}$$

Product of **Sum Product of Maxterms**

Ex 2.4

$$F = A + B'C$$

I - \neg \wedge \vee \rightarrow \wedge

$$\begin{aligned} A &= A(B + B') = AB + AB' = AB(C+C') + AB'(C+C') \\ &= ABC + ABC' + AB'C + AB'C' = m_7 + m_6 + m_5 + m_4 \\ B'C &= (A+A')B'C = AB'C + A'B'C = m_5 + m_1 \\ &= m_1 + m_4 + m_5 + m_6 + m_7 \\ F(A, B, C) &= \Sigma(1, 4, 5, 6, 7) \end{aligned}$$

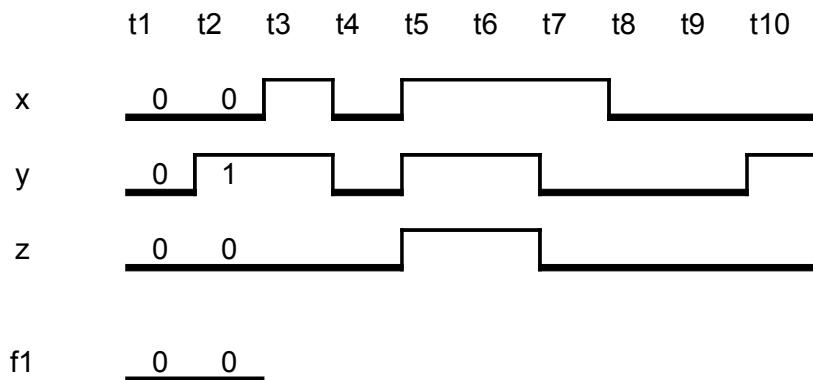
	x	y	z	term
0	0	0	0	0
1	0	0	1	1
2	0	1	0	0
3	0	1	1	0
4	1	0	0	1
5	1	0	1	0
6	1	1	0	0
7	1	1	1	1

$$\begin{aligned} m_1 + m_4 + m_7 &= f_1 \\ m_0 + m_2 + m_3 + m_5 + m_6 &= f_1' \end{aligned}$$

0	0	0	1	0	1	1		
		x	0	1	0	1		
0	0	0	1	0	1	1		
0	0	0	0	0	0	0		
0	1	0	1	1	0	0		
0	0	0	0	0	0	0		
0	1	1	0	1	1	1		
32	16			7				

HW

(1) Complete the waveform of the function f1



$$f_1 = x'y'z + xy'z' + xyz = m_1 + m_4 + m_7$$

HW

(2) Read the following tutorial

<http://www4.wittenberg.edu/academics/>

google search: Multiplication of binary integer pdf wittenberg

What are the values stored in the variable n and m?

multiplicand, multiplier

What is the reason of shifting n and m?

Show the result of execution of the binary multiplication code.

n = 0 1 1 0 1 1 0 1

n>>1 0 0 1 1 0 1 1 0

n>>1 0 0 0 1 1 0 1 1

0xff 1 1 1 1 1 1 1 1

0x33 0 0 1 1 0 0 1 1

n =	0 1 1 0 1 1 0 1							
& 0x01	0 0 0 0 0 0 0 1							
<hr/>								