Binary Arithmetic in C (7A)

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Make a binary string

```
//.....................................
// n : bit width
// 1 << n : shift left by n bits (2^n)
// mask   : n bit filled with all one's (2^n -1)
//.....................................
#define nn 3
int n = nn;
int mask = (1 << nn) - 1;
```

```
// make a binary string from the given num
void bstr(int num, int nbit, char * s)
{
  int i, j;

  for (i=0; i<nbit; ++i) {  // i-th bit
    j = nbit -i -1;         // j-th position in s[]
    if (num & (1 << i)) s[j] = '1';  // the i-th bit of
num
    else s[j] = '0';
  }
  s[nbit] = '\0';
}
```

Get a 2's complementary number

```
// make a 2's complementary number from
unsigned number.
int snum(int x, int nbit)
{
    int num;

    if (x < (1 << (nbit-1))) num = x;
    else num = x - (1 << nbit);

    return (num);
}
```

List 3-bit binary numbers

```
ui =    0 i=   +0   000
ui =    1 i=   +1   001
ui =    2 i=   +2   010
ui =    3 i=   +3   011
ui =    4 i=   -4   100
ui =    5 i=   -3   101
ui =    6 i=   -2   110
ui =    7 i=   -1   111
```

```
void main()
{

  unsigned char ui, uj;
  signed char i, j;
  char s[10];

  int x, y, z;


  for (x=0; x<(1<<n); ++x) {
    // ui: unsigned number
    ui = x;

    // i: signed 2's complement number
    i = snum(x, n);

    // s: binary string of the given number i
    bstr(i, n, s);

    printf("ui = %4d i= %+4d  %4s \n", mask & ui, i, s);
  }
```

Addition Table for 3-bit binary numbers

```
for (x=0; x<(1<<n); ++x) {
  for (y=0; y<(1<<n); ++y) {
    ui = x;
    uj = y;
    z = mask & (ui + uj);
    bstr(z, n+1, s);

    printf(" %4s(%+1d)",  s, snum(z, n));
  }
  printf("\n");
 }


}
```

```
0000(+0) 0001(+1) 0010(+2) 0011(+3) 0100(-4) 0101(-3) 0110(-2) 0111(-1)
0001(+1) 0010(+2) 0011(+3) 0100(-4) 0101(-3) 0110(-2) 0111(-1) 0000(+0)
0010(+2) 0011(+3) 0100(-4) 0101(-3) 0110(-2) 0111(-1) 0000(+0) 0001(+1)
0011(+3) 0100(-4) 0101(-3) 0110(-2) 0111(-1) 0000(+0) 0001(+1) 0010(+2)
0100(-4) 0101(-3) 0110(-2) 0111(-1) 0000(+0) 0001(+1) 0010(+2) 0011(+3)
0101(-3) 0110(-2) 0111(-1) 0000(+0) 0001(+1) 0010(+2) 0011(+3) 0100(-4)
0110(-2) 0111(-1) 0000(+0) 0001(+1) 0010(+2) 0011(+3) 0100(-4) 0101(-3)
0111(-1) 0000(+0) 0001(+1) 0010(+2) 0011(+3) 0100(-4) 0101(-3) 0110(-2)
```

Laplace Equation

References

[1] http://en.wikipedia.org/
[2] http://planetmath.org/
[3] M.L. Boas, “Mathematical Methods in the Physical Sciences”