# Applicatives Overview (3A)

Copyright (c) 2016 - 2018 Young W. Lim.
Permission is granted to copy, distribute and/or modify this document under the terms of the GNU Free Documentation License, Version 1.2 or any later version published by the Free Software Foundation; with no Invariant Sections, no Front-Cover Texts, and no Back-Cover Texts. A copy of the license is included in the section entitled "GNU Free Documentation License".
Please send corrections (or suggestions) to youngwlim@hotmail.com.
This document was produced by using LibreOffice.

#### Based on

http://learnyouahaskell.com/making-our-own-types-and-typeclasses#the-functor-typeclass

http://learnyouahaskell.com/functors-applicative-functors-and-monoids

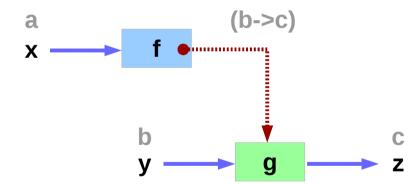
Haskell in 5 steps

https://wiki.haskell.org/Haskell\_in\_5\_steps

### Currying

Currying recursively transforms
a function that takes <u>multiple arguments</u>
into a function that takes just a <u>single argument</u> and
returns <u>another function</u> if any arguments are still needed.

$$f:: a -> b -> c \implies f:: a -> (b -> c)$$



https://wiki.haskell.org/Currying http://learnyouahaskell.com/functors-applicative-functors-and-monoids

#### **Curry & Uncurry**

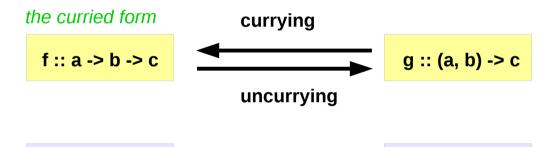
 $f :: a \rightarrow b \rightarrow c$  is the curried form of  $g :: (a, b) \rightarrow c$ 

$$f x y = g (x,y)$$

the curried form is usually more convenient because it allows partial application.

all functions are considered curried

all functions take just one argument



https://wiki.haskell.org/Currying

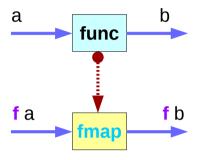
fxy

g (x,y)

## Functor typeclass – instances

#### class Functor f

instance Functor Maybe instance Functor []



function fmap function func type constructor f

f is a type constructor taking one type parameter

Maybe instance of the Functor typeclass
[] instance of the Functor typeclass

http://learnyouahaskell.com/making-our-own-types-and-typeclasses#the-functor-typeclass

#### The Functor Typeclass

```
class Functor f where
```

```
fmap :: (a -> b) -> f a -> f b
```

If a type **f** is an <u>instance</u> of **Functor**, **fmap** can be used to apply a function of the type (a -> b) to values of a type **a** in it (**f a**).

fmap promotes functions (a -> b)

to act on functorial values. (f  $a \rightarrow f b$ )

fmap id = id -- 1st functor law fmap (g . h) = fmap g . fmap h -- 2nd functor law

g::b->c

h :: a -> b

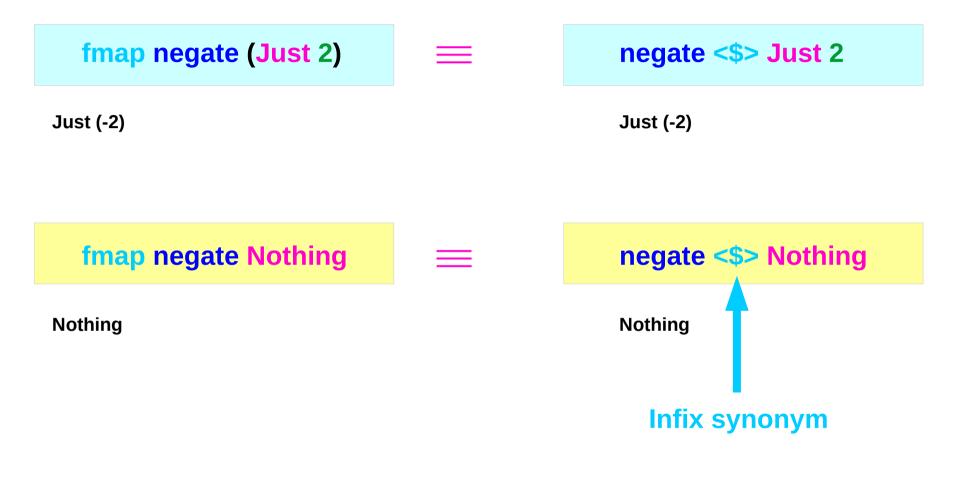
g.h::a->c

To ensure **fmap** works sanely,

any instance f of Functor

must comply with the above two laws

#### Examples of fmap over the Maybe Functor instance



#### Applying two argument functions

#### Problem:

to apply a function of two arguments to functorial values

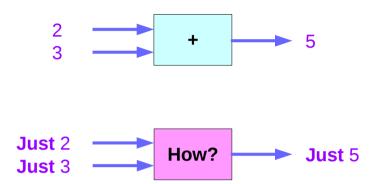
Ex: to sum Just 2 and Just 3

The brute force approach would be <a href="mailto:extracting">extracting</a> the values from the **Maybe** wrapper.

- we have to do tedious checks for Nothing
- extracting the value might is <u>not possible</u>
   for functors like **IO**

#### **Partial application**

• use **fmap** to partially apply (+) to the first argument:



#### **Partial Application**

```
Prelude> :t (+)
(+) :: Num a => a -> a -> a

Prelude> :t (+) <$> Just 2
(+) <$> Just 2 :: Num a => Maybe (a -> a)

Functions wrapped in Maybe

(+) <$> Just 2

Just (2+)
```

```
Prelude> (<$> Just 3) <$> (+) <$> Just 2

Just (Just 5)

(<$> Just 3) <$> (+) <$> Just 2

(<$> Just 3) <$> Just (2+)

Just( (2+) <$> Just 3)

Just (Just 5)
```

#### **Partial Application**

```
Prelude> :t (<$> Just 3)
(<\$> Just 3) :: Num a => (a -> b) -> Maybe b
Prelude> (<$> Just 3) (*3)
Just 9
Prelude> (<$> Just 3) (+3)
Just 6
Prelude>:t (+)
(+) :: Num a => a -> a -> a
Prelude> :t (+) <$> Just 2
(+) <$> Just 2 :: Num a => Maybe (a -> a)
```

```
Prelude> (<$> Just 3) <$> (+) <$> Just 2

Just (Just 5)

(<$> Just 3) <$> (+) <$> Just 2

(<$> Just 3) <$> Just (2+)

Just( <$> Just 3 (2+))

Just( (2+) <$> Just 3 )

Just (Just 5)
```

#### <\*> Operator

Just 5

Just 3 :: f a

Just 5 :: f b

$$(<*>)$$
 :: Applicative f => f (a -> b) -> f a -> f b

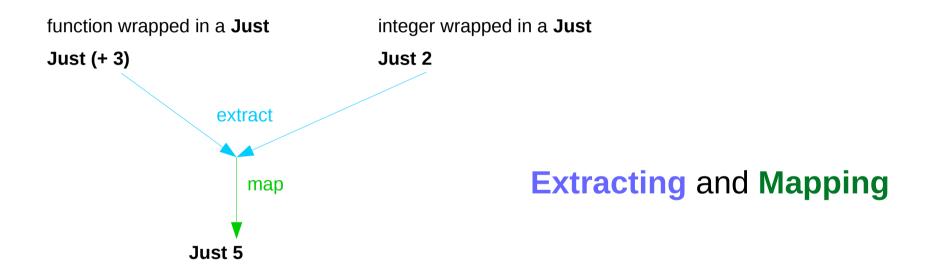
Just 5

### **Applicative Style**

(<\*>) is one of the methods of **Applicative** the type class of applicative functors - functors that support function application within their contexts.

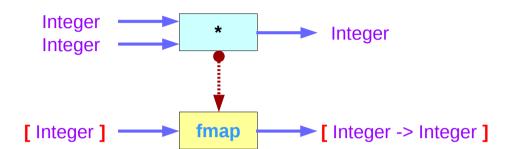
Expressions (+) <\$> Just 2 <\*> Just 3 are said to be written in applicative style, which look like regular function application while working with a functor.

#### <\*> Application of a function

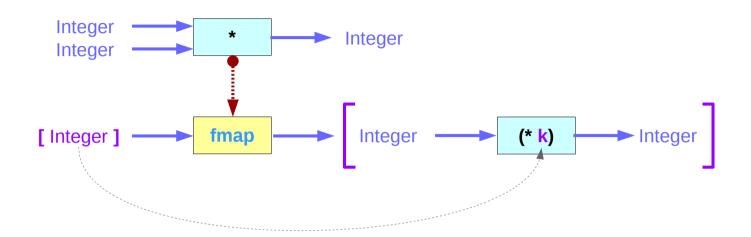


#### Just 5

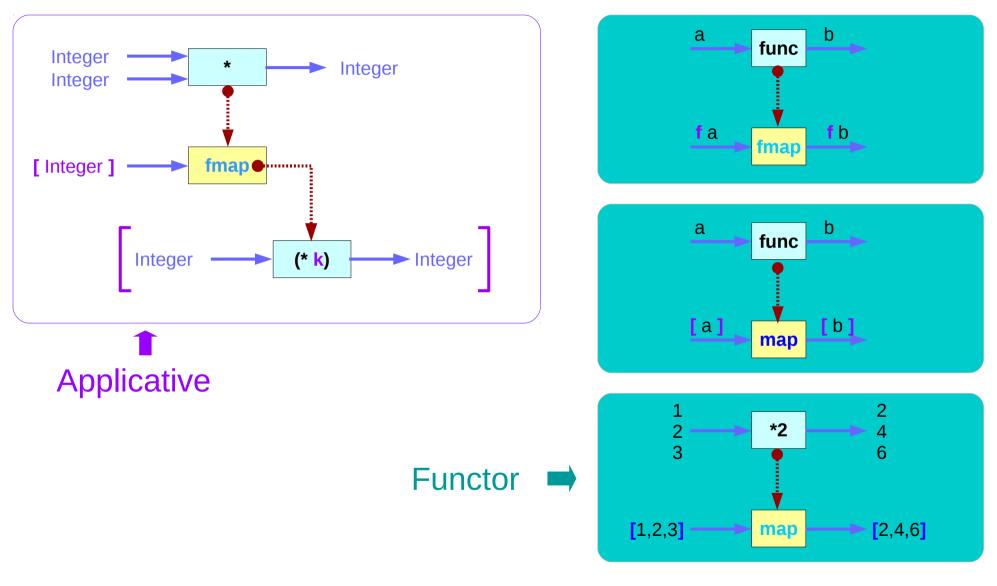
## Mapping functions over the Functor [ ] (1)



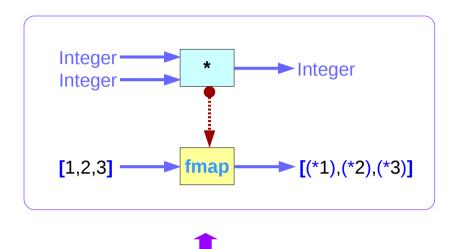
## Mapping functions over the Functor [ ] (2)



### Mapping functions over the Functor [ ] (3)



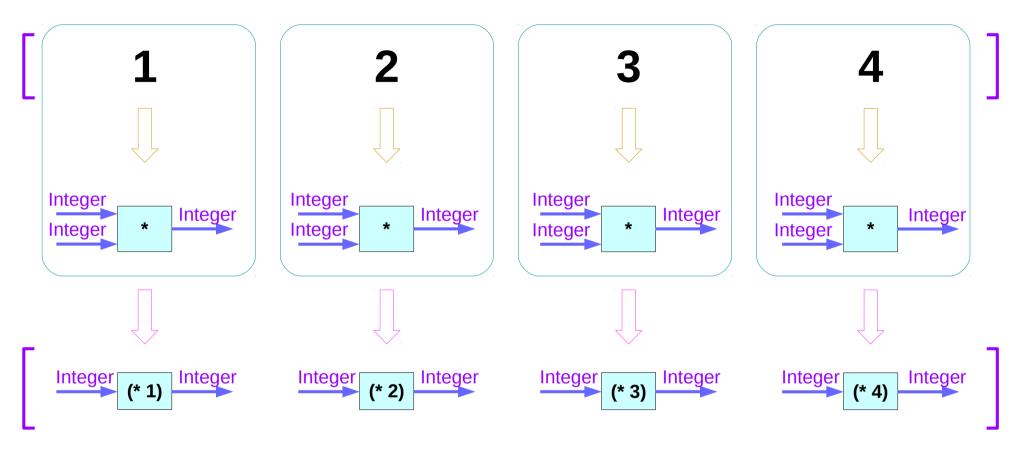
## Mapping functions over the Functor [ ] (4)



**Applicative** 

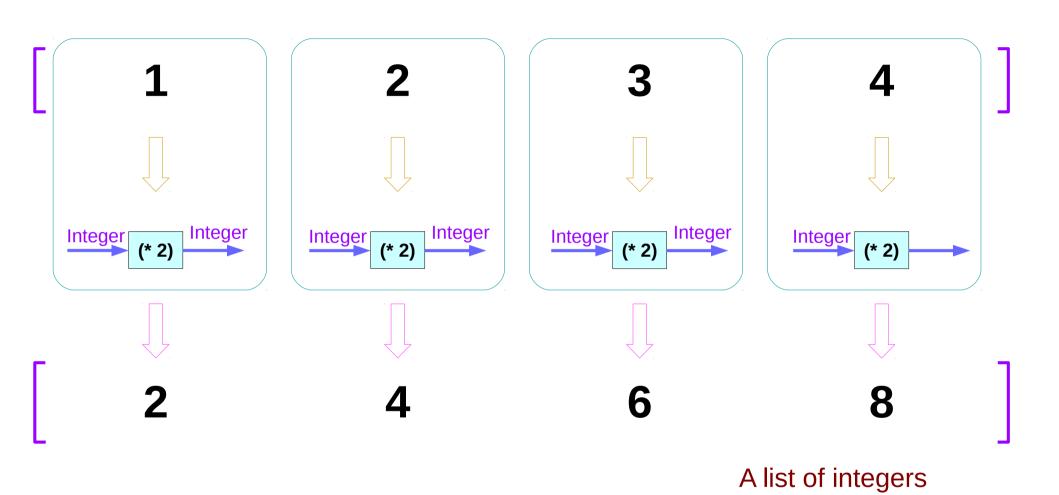
Functor (1,2,3) (2,4,6)

## Applicative : Mapping functions

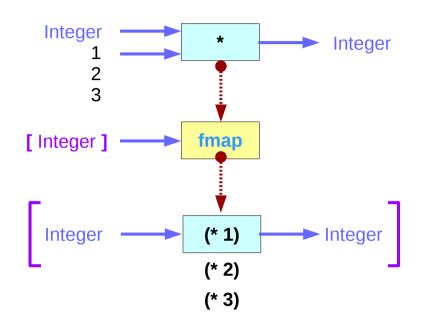


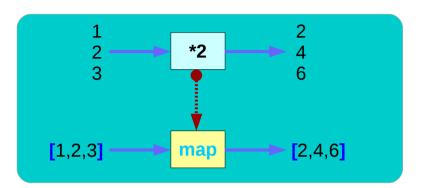
A list of functions

#### Functor: Mapping values



#### Applicatives vs. Functors





### Double applications of fmap (1)

ghci> let a = fmap(\*)[1,2,3,4]

ghci>:ta

a :: [Integer -> Integer]

ghci> fmap (\f -> f 9) a [9,18,27,36]

### Double applications of fmap (2)

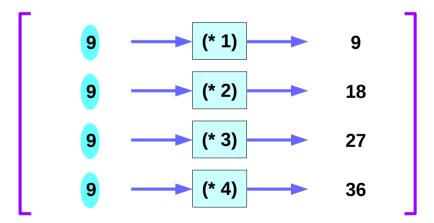
```
ghci> let a = fmap (*) [1,2,3,4]

1^{st} fmap

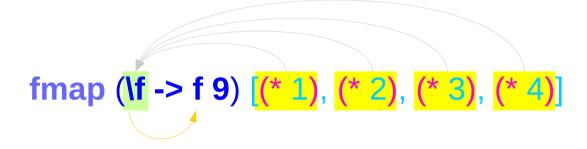
ghci> fmap (\f -> f 9) a

[9,18,27,36]

2^{nd} fmap
```

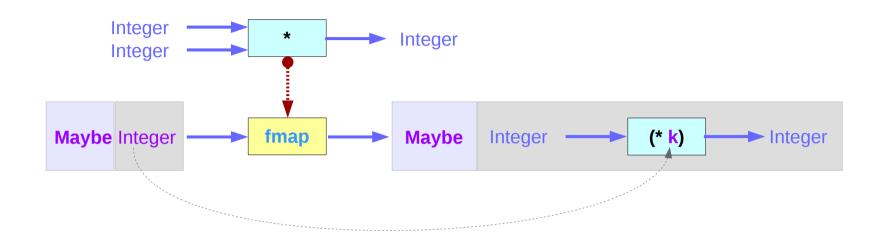


#### Applications of **fmap**

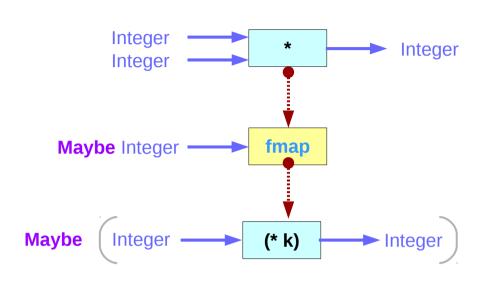


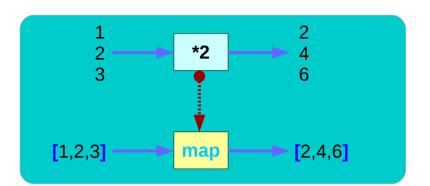
[9,18,27,36]

#### Mapping functions over the Functor Maybe (1)



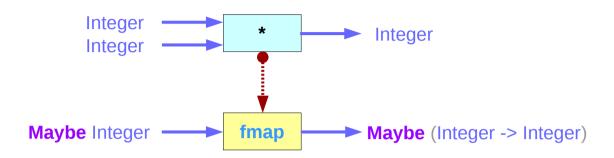
#### Mapping functions over the Functor Maybe (2)

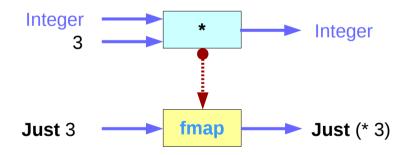






### Mapping functions over the Functor Maybe (3)



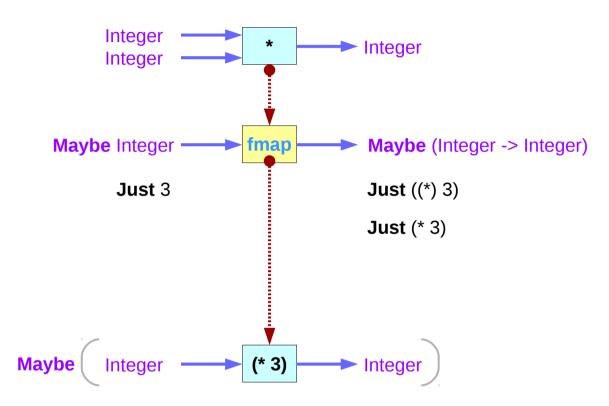


#### Function wrapped in Just



function wrapped in a **Just** 

**Just** (\* 3)

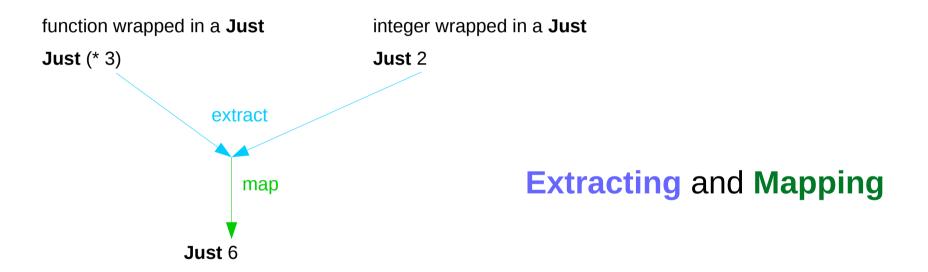


integer wrapped in a **Just** 

Just 2

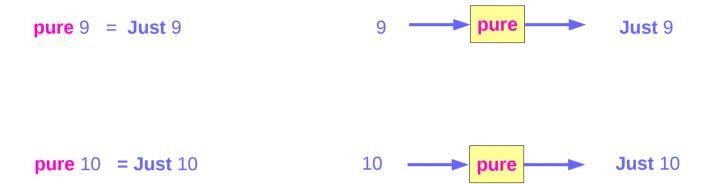
#### <\*> Application of a function

#### Just (\* 3) <\*> Just 2



#### Just 6

#### Default Container Function Pure



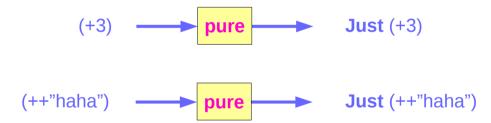
to wrap an **integer** 

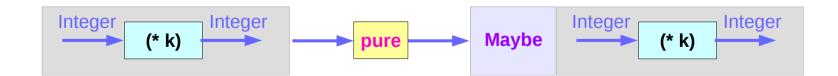
#### Default Container Function Pure

#### pure (+3) = Just (+3)

#### to wrap a function

pure (++"haha") = Just (++"haha")



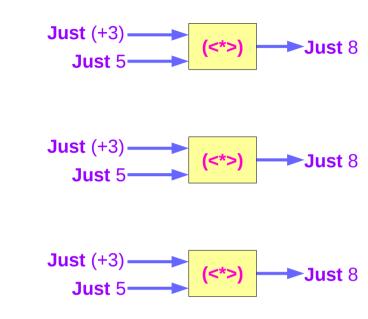


## Applicative Functor Apply <\*> Examples (1)

Prelude> Just (+3) <\*> Just 9 **▶Just** 12 Just 12 Prelude> pure (+3) <\*> Just 10 **▶Just** 13 **Just** 10 Just 13 Prelude> pure (+3) <\*> Just 11 Just (+3)-**►Just** 14 **Just 11** Just 12 Prelude > Just (++"hahah") <\*> Nothing Just (++"haha") -(<\*>) Nothing **Nothing Nothing** Prelude> Nothing <\*> Just "woot" **Nothing** Nothing **Nothing** Just "woot"

### Applicative Functor Apply <\*> Examples (2)

```
Prelude> (+) <$> Just 3 <*> Just 5
Just 8
Prelude> pure (+) <*> Just 3 <*> Just 5
Just 8
Prelude> Just (+) <*> Just 3 <*> Just 5
Just 8
Prelude> :t (+) <$> Just 3
(+) <$> Just 3 :: Num a => Maybe (a -> a)
Prelude>:t Just (+3)
Just (+3) ::Num a => Maybe (a -> a)
```



### Applicative Functor Apply <\*> Examples (3)

```
Prelude> [ (+), (*) ] <*> [ 2 ] <*> [ 5 ]
[7,10]
                          (+2) (*2)
5 5 [7,10]
Prelude> [ (+), (*) ] <*> [ 2,3 ] <*> [ 5 ]
7,8,10,15
                   Prelude> [ (+), (*) ] <*> [ 2,3 ] <*> [ 5,6 ]
[7,8,8,9,10,12,15,18]
```

#### References

- [1] ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf
- [2] https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf