# Displacement Sensor (5A)

- Displacement Sensor Type
- Displacement Sensor Characteristics

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# Displacement Sensor Type

Displacement Type	Displacement Sensor	Physical Effect
Linear	Potentiometer	R (resistance)
	LVDT	L (inductance)
	Capacitive	C (capacitance)
Angular	Potentiometer	R (resistance)
	RVDT Synchro Resolver	L (inductance)
	Capacitive	C (capacitance)
	Encoder	

# Potentiometer Types

#### **Resistive Potentiometer**

#### **Magneto-resistive Potentiometer**

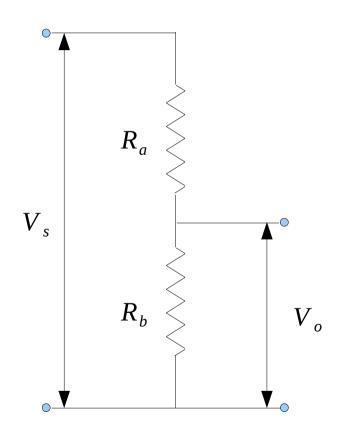
• magnetic field => resistance

#### **Photo Potentiometer**

- incident light => resistance
- PSD (Position Sensitive Device)
- PIN photo-diode semiconductor

# Potentiometer (1)

### **Voltage Divider**



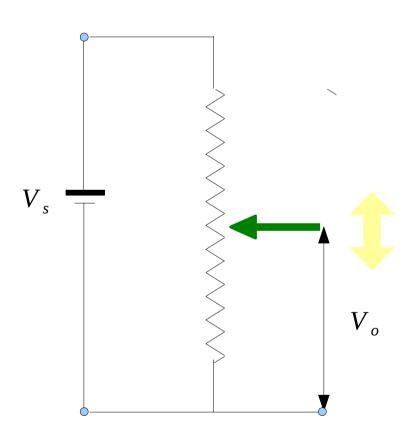
$$V_o = \frac{R_b}{R_a + R_b} \cdot V_s$$

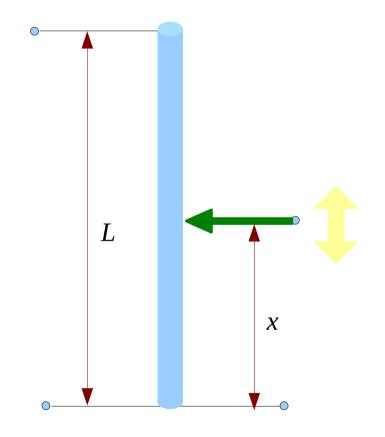
$$R_a + R_b \propto L$$
 
$$R_b \propto x \quad (displacement)$$

# Potentiometer (2)

### **Voltage Divider**

$$V_o = \frac{x}{L} \cdot V_s = Kx$$





# Inductive Displacement Sensor Types

#### **LVDT** (Linear Variable Differential Transformer)

#### **RVDT** (Rotary Variable Differential Trnasformer)

- primary coil
- secondary coil
- moving iron core

#### **Synchro**

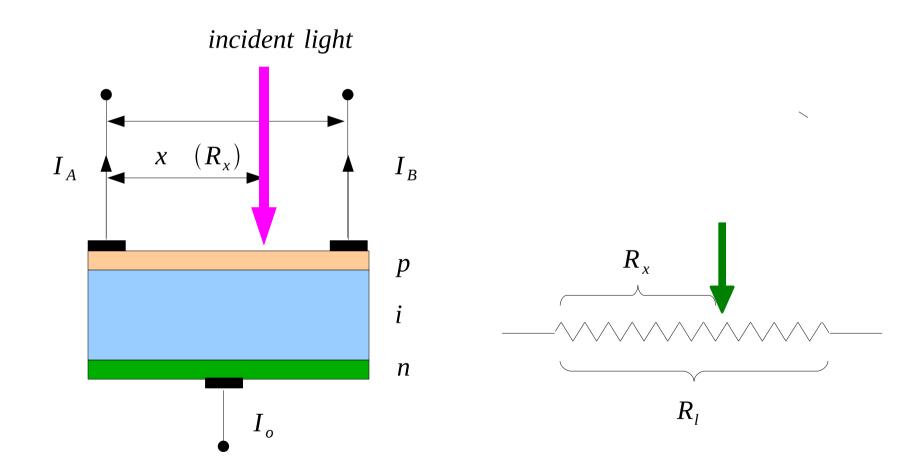
- Rotor primary coil
- Stator 3 secondary coils (180 deg apart)

•

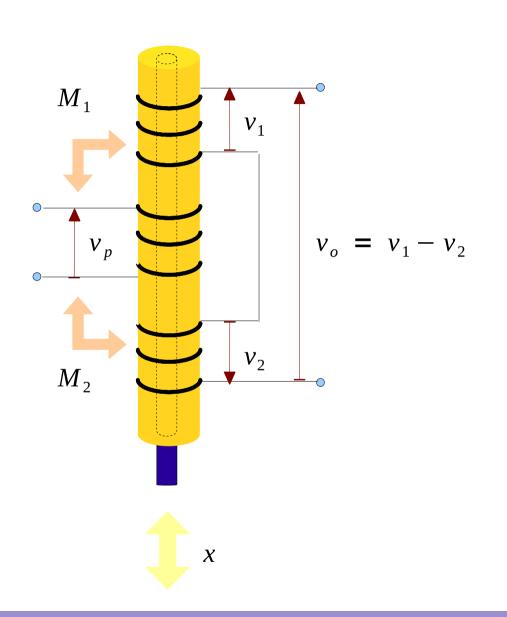
#### Resolver

- Rotor primary coil
- Stator 2 secondary coils (90 deg apart)

### Position Sensitive Device



### Inductive Displacement Sensor – LVDT



$$v_1 = M_1 \frac{i_p}{dt}$$

$$v_2 = M_2 \frac{i_p}{dt}$$

$$v_o = v_1 - v_2 = M_1 \frac{i_p}{dt} - M_2 \frac{i_p}{dt}$$

$$v_o = (M_1 - M_2) \frac{i_p}{dt}$$

# Capacitive Displacement Sensor Types

### **Variable Distance Displacement Sensor**

• x is varying

$$C(x) = \frac{\epsilon_r \epsilon_o A}{x}$$

#### **Variable Area Displacement Sensor**

• A is varying

### Variable <u>Dielectric</u> Displacement Sensor

ε<sub>r</sub> is varying

# Capacitive Displacement Sensor – Distance

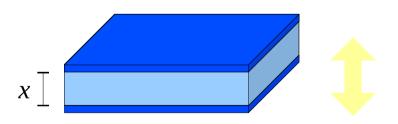
### Variable <u>Distance</u> Displacement Sensor

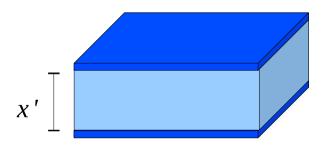
• x is varying

$$\frac{dC(x)}{dx} = -\frac{\epsilon_r \epsilon_o A}{x^2}$$

$$C(x) = \frac{\epsilon_r \epsilon_o A}{x}$$

$$\frac{dC(x)}{C} = -\frac{dx}{x}$$



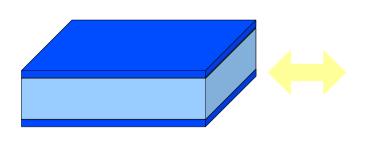


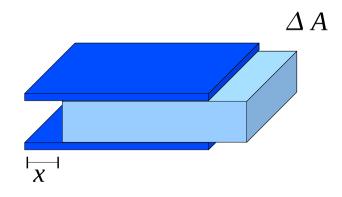
# Capacitive Displacement Sensor – Area

### **Variable Area Displacement Sensor**

• A is varying

$$C(x) = \frac{\epsilon_r \epsilon_o (A - wx)}{x}$$



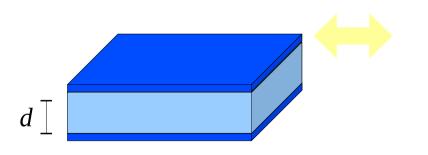


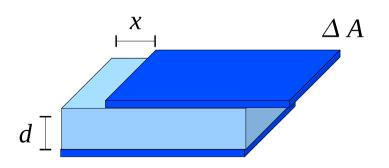
# Capacitive Displacement Sensor – Dielectric

#### Variable <u>Dielectric</u> Displacement Sensor

• A is varying

$$C(x) = \frac{\epsilon_0 w}{d} \left[ \epsilon_{r2} l - (\epsilon_{r2} - \epsilon_{r1}) x \right]$$





# Capacitive Displacement Sensor

#### Thermo-electricity:

- a temperature difference crates an electrical potential
- an electrical potential creates a temperature difference

#### **Pyro-electricity:**

- generates a temporary electrical potential when certain materials are heated or cooled
- the opposite effect is called electro-caloric effect

# **Rotary Encoder**

- Incremental Type
- Absolute Type

- Optical Encoder
- Magnetic Encoder

#### References

- [1] http://en.wikipedia.org/
- [2] Nam Ki Min, Sensor Electronics, Dong-il Press